

CHAPTER-2 ( Differentiation )

Name \_\_\_\_\_

**PLEASE SHOW YOUR WORK AS NEATLY AS POSSIBLE :**

- 1) Find the first and the second derivatives of the following functions :

a)  $f(x) = \frac{5 \sin(x)}{3} - x$

b)  $y = \frac{x}{2} - \frac{\sin(2x)}{4}$

- 2) Find the derivative :

a)  $y = \sec^2(\Delta x)$

b)  $y = \sin^2\left(\frac{x}{2}\right)$

3)  $f(x) = \frac{2}{\sqrt{x+1}}$

a) Find the derivative,  $f'(x)$ .

b) Find the point on  $f$  where the slope of the tangent is  $-\frac{1}{8}$ .

4) Find all points  $(x, f(x))$  on the graph of Let  $f(x) = \frac{3x^2}{2} - x^3 + 13$

a) Find the derivative.

b) Find all points  $(x, f(x))$  on the graph of  $f(x)$  with tangent lines parallel to the line  $8x - 2y = 1$

5) Given  $f(x) = \sqrt{x^2 + 2}$

a) Find the derivative,  $f'(x)$ .

b) Find the equation of the tangent line at  $x = 1$

6) Given:  $f(x) = 1 - \cos(2x) + \cos^2 x$

a) Find the derivative,  $f'(x)$ .

b) Determine the values of  $x$  in the interval  $[0, 2\pi)$  at which the graph of  $f(x)$  has a horizontal tangent lines.

7) **Given :**  $6x^2y - \Delta \cos y = 7\Delta$

a) **Find**  $dy/dx$

b) **Find the equation of the normal line at the point**  $(1, \Delta)$

- 8) A 17- ft ladder is leaning against the side of a house. The top of the ladder is sliding down the house at rate of 5 ft/sec.
- a) Determine how fast the bottom of the ladder is sliding away when the top of the ladder is 8 feet from the ground.
  - b) At what rate is the angle  $\theta$  between the ladder and the ground is changing then.

- 9) A cube's surface area increases at a rate of  $72 \text{ in}^2/\text{sec}$  . At what rate is the cube's Volume changing when the side's length is 3 inches ?

- 10) A water tank has the shape of an inverted right circular cone. The container has a radius of 2 m and a height of 4 m . If water is being pumped into the tank at a rate of  $2 \text{ m}^3/\text{sec}$ . Find the rate at which water level is rising when the water is 3 m deep.